

$$1. \quad \Delta u = \cos \varphi, \quad r > 3, \\ u(3, \varphi) = 3 \sin 2\varphi.$$

$$2. \quad \Delta u = 0, \quad 0 < x < \pi, \quad 0 < y < \frac{\pi}{2}, \quad \text{если } u(0, y) = 0, u(\pi, y) = 0, u(x, 0) = 0, u(x, \frac{\pi}{2}) = \sin 3x$$

$$3. \quad \Delta u = 0, \quad -\infty < x < \infty, \quad -2\pi < y < 0; \quad u(x, -2\pi) = 0, \quad u(x, 0) = 1, \quad \text{при } x < 1; \quad u(x, 0) = 0, \quad \text{при } x \geq 1$$

$$4. \quad \begin{cases} u_{tt} = u_{xx} - \sin 3x, \quad t > 0, \quad 0 < x < \frac{\pi}{2}; \\ u(0, t) = t, \quad u_x(\frac{\pi}{2}, t) = 0, \\ u(x, 0) = 2 \sin 3x - \sin x, \\ u_t(x, 0) = \sin x + 1. \end{cases}$$

$$5. \quad u_{tt} = 9u_{xx}, \quad 0 < x < \infty, \quad t > 0$$

$$u_x(0, t) = 0, \quad u(x, 0) = \begin{cases} \sin x, & x \in [0; \pi] \\ 0, & x \notin [0; \pi] \end{cases}, \quad u_t(x, 0) = 0. \quad \text{Найти } u(\frac{\pi}{4}, t) \text{ и нарисовать график.}$$

$$6. \quad u_{tt} = 4u_{xx}, \quad t > 0, \quad x > 0;$$

$$u_x(0, t) = 0 \quad u(x, 0) = \sin x \quad u_t(x, 0) = 2 \cos x.$$

Описать процесс колебаний. Построить профиль струны в момент времени $t = \frac{\pi}{4}$.